# MA383: Introduction to Modern Algebra 

Fall 2022 Itinerary

## Wednesday, August 17 (Week 1)

Review of Set Operations and the Basics of Logic

## Friday, August 19

The Principle of Mathematical Induction and the Division Algorithm
Quiz: Set Operations and the Basics of Logic

Monday, August 22 (Week 2)
The Integers Modulo $n$ and Rigid Motions
Quiz: the Principle of Mathematical Induction and the Division Algorithm

## Group Theory

Wednesday, August 24
Groups (Definitions and Examples)
Quiz: the Integers Modulo $n$ and Rigid Motions

Friday, August 26
Groups (Basic Properties and Subgroups)
Quiz: Groups (Definitions and Examples)

Monday, August 29 (Week 3)
Cyclic Groups
Quiz: Groups (Basic Properties and Subgroups)

## Wednesday, September 1

Complex Numbers as a Group Under Multiplication
Quiz: Cyclic Groups

## Friday, September 2

The Symmetric Group on $n$ Letters
Quiz: Complex Numbers as a Group Under Multiplication

## Monday, September 5 (Week 4)

Labor Day

## Wednesday, September 7

Dihedral Groups
Quiz: the Symmetric Group on $n$ Letters

Friday, September 9
Cosets and Lagrange's Theorem
Quiz: Dihedral Groups

Monday, September 12 (Week 5)
Quotient Groups and Normal Subgroups
Quiz: Cosets and Lagrange's Theorem

Wednesday, September 14
Group Homomorphisms and Cayley's Theorem
Quiz: Quotient Groups and Normal Subgroups

Friday, September 16
The Group Isomorphism Theorems
Quiz: Group Homomorphisms and Cayley's Theorem

Monday, September 19 (Week 6)
External and Internal Direct Products
Quiz: the Group Isomorphism Theorems

Wednesday, September 21
Finite Abelian Groups
Quiz: External and Internal Direct Products

Friday, September 23
Finitely Generated Abelian Groups and the Smith Normal Form
Quiz: Finite Abelian Groups

Monday, September 26 (Week 7)
Group Actions and the Class Equation
Quiz: Finitely Generated Abelian Groups and the Smith Normal Form

## Wednesday, September 28

Sylow's Theorems
Quiz: Group Actions and the Class Equation

Friday, September 30
Sylow's Theorems (Applications)
Quiz: Sylow's Theorems

Monday, October 3 (Week 8)
Exam I Review
Quiz: Sylow's Theorems (Applications)

Wednesday, October 5
Exam I

Friday, October 7
Fall Break

## Ring Theory

Monday, October 10 (Week 9)
Rings, Ring Homomorphisms, Ideals, and Quotient Rings

## Wednesday, October 12

The Ring Isomorphism Theorems
Quiz: Rings, Ring Homomorphisms, Ideals, and Quotient Rings

Friday, October 14
Integral Domains, Fields, and Prime and Maximal Ideals
Quiz: the Ring Isomorphism Theorems

Monday, October 17 (Week 10)
The Chinese Remainder Theorem
Quiz: Integral Domains, Fields, and Prime and Maximal Ideals

Wednesday, October 19
Extension, Contraction, and Oka Families
Quiz: the Chinese Remainder Theorem

## Friday, October 21

Polynomial Rings and Polynomial Long Division
Quiz: Extension, Contraction, and Oka Families

Monday, October 24 (Week 11)
Irreducibility of Polynomials
Quiz: Polynomial Rings and Polynomial Long Division

Wednesday, October 26
Euclidean Domains
Quiz: Irreducibility of Polynomials

Friday, October 28
Principal Ideal Domains (PIDs)
Quiz: Euclidean Domains

Monday, October 31 (Week 12)
Unique Factorization Domains (UFDs)
Quiz: Principal Ideal Domains (PIDs)

## Wednesday, November 2

Polynomial Rings over UFDs
Quiz: Unique Factorization Domains (UFDs)

Friday, November 4
Fields of Fractions and Localization
Quiz: Polynomial Rings over UFDs

Monday, November 7 (Week 13)
Exam II Review
Quiz: Fields of Fractions and Localization

## Wednesday, November 9

Exam II

# Field Theory 

Friday, November 11
Roots of Polynomials and Field Extensions

Monday, November 14 (Week 14)
Finite Extensions
Quiz: Roots of Polynomials and Field Extensions

Wednesday, November 16
Splitting Fields of Polynomials and Algebraic Closure
Quiz: Finite Extensions

Friday, November 18
Finite Fields
Quiz: Splitting Fields of Polynomials and Algebraic Closure

Monday, November 21 (Week 15)
Separable Extensions
Quiz: Finite Fields

Wednesday, November 23
Thanksgiving Break

Friday, November 25
Thanksgiving Break

Monday, November 28 (Week 16)
Field Automorphisms
Quiz: Separable Extensions

Wednesday, November 30
The Galois Group
Quiz: Field Automorphisms

## Friday, December 2

The Fundamental Theorem of Galois
Quiz: the Galois Group

